

### Solve & Discuss It!

Jamal can run 1 mile in 5.05 minutes. If Jamal maintains this pace during a 5-kilometer (5K) race, he expects to break the course record of 15.25 minutes. Is Jamal's expectation reasonable? Explain.



**Be Precise** How can you convert 5 kilometers to miles?

#### Lesson 3-4

##### Describe Proportional Relationships: Constant of Proportionality

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**I can...**  
use the constant of proportionality in an equation to represent a proportional relationship.

**Focus on math practices**

**Reasoning** Assuming that Jamal runs at a constant rate, how does his pace describe the time it takes him to finish a race of any length?

### Essential Question

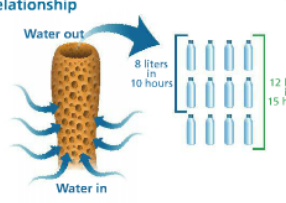
How can you represent a proportional relationship with an equation?

Interactive Activities

#### EXAMPLE 1 Write an Equation to Represent a Proportional Relationship

A sponge is an example of a *filter feeder*. It takes in food by filtering water through its body. The sponge maintains a constant flow of water through its body.

What is an equation that represents the proportional relationship between the time and the amount of water filtered?



The **constant of proportionality** is the constant multiple that relates proportional quantities  $x$  and  $y$ . It is the value of the ratio  $\frac{y}{x}$  and is represented by  $k$ .

Make a table to find the constant of proportionality.

Hours ( $x$ )	Liters ( $y$ )	Liters/Hours ( $\frac{y}{x}$ )
10	8	$\frac{8}{10} = 0.8$
15	12	$\frac{12}{15} = 0.8$

The constant of proportionality,  $k$ , is 0.8.

You can use  $k$  to write an equation that represents a proportional relationship.

$$k = \frac{y}{x}$$

$$kx = y$$

$$y = kx$$

You can use an equation in the form  $y = kx$  to represent any proportional relationship.

Use the equation to represent the relationship between time and the amount of water filtered.

$$y = 0.8x$$

**Try It!**

Maria made two batches of fruit punch. The table at the right shows how many quarts of juice she used for each batch. Write an equation that relates the proportional quantities.

Apple Juice ( $x$ )	Grape Juice ( $y$ )	Grape Juice/Apple Juice ( $\frac{y}{x}$ )
5	8	<input type="text"/>
10	16	<input type="text"/>


**Convince Me!** How does the equation change if the amount of grape juice is the independent variable,  $x$ , and the amount of apple juice is the dependent variable,  $y$ ?

The constant of proportionality is .

An equation that represents this proportional relationship is  $y = \text{} x$ .

**EXAMPLE 2** Solve Problems Using an Equation

1 inch = 2.54 centimeters. How many centimeters long is an 18-inch ruler?



**STEP 1** Write an equation to represent this relationship.

centimeters  $\swarrow$  inches  
 $y = kx$   
 ↑  
 constant multiple or constant of proportionality  
 $y = 2.54x$

**STEP 2** Use the equation to find the length of the ruler in centimeters.


$y = 2.54x$   
 $y = 2.54(18)$   
 $y = 45.72$   
 The ruler is 45.72 centimeters long.

**Try It!**

A florist sells a dozen roses for \$35.40. She sells individual roses for the same unit cost. Write an equation to represent the relationship between the number of roses,  $x$ , and the total cost of the roses,  $y$ . How much would 18 roses cost?

**EXAMPLE 3** Determine Whether  $y = kx$  Describes a Situation

Can you represent the total cost,  $y$ , for admission and  $x$  rides at the amusement park using an equation in the form  $y = kx$ ? Explain.



**STEP 1** Make a table that shows the total cost.

Rides	Cost
1	\$25
2	\$30
3	\$35

**STEP 2** Compare the ratios to determine whether the relationship is proportional.

$\frac{\$25}{1} = \$25$   
 $\frac{\$30}{2} = \$15$   
 $\frac{\$35}{3} = \$11.67$

This relationship is not proportional, so it cannot be represented with an equation of the form  $y = kx$ .

**Try It!**

Balloon A is released 5 feet above the ground. Balloon B is released at ground level. Both balloons rise at a constant rate. Which situation can you represent using an equation of the form  $y = kx$ ? Explain.

Balloon A		Balloon B	
Time (s)	Height (ft)	Time (s)	Height (ft)
1	9	1	4
2	13	2	8
3	17	3	12

**KEY CONCEPT**

Two proportional quantities  $x$  and  $y$  are related by a constant multiple, or the constant of proportionality,  $k$ . You can represent a proportional relationship using the equation  $y = kx$ .

$y = kx$

**Do You Understand?**

- Essential Question** How can you represent a proportional relationship with an equation?
- Generalize** How can you use an equation to find an unknown value in a proportional relationship?
- Reasoning** Why does the equation  $y = 3x + 5$  NOT represent a proportional relationship?

**Do You Know How?**

- Determine whether each equation represents a proportional relationship. If it does, identify the constant of proportionality.
  - $y = 0$   ~~$k = 0$~~  **NOT proportional**
  - $y = 1,000x$   
 $k = 1,000$
  - $y = \dots$  **Not proportional**
- The manager of a concession stand estimates that she needs 3 hot dogs for every 5 people who attend a baseball game. If 1,200 people attend the game, how many hot dogs should the manager order?

\* no adding or subtracting

a) 

x	y
2	-1
4	0
6	+1

 -2  
?  
+6

$y = kx$

$6c = \$15$   
 $k = \$2.50$   
 $y = 2.50x$

$\frac{\$15 \div 3}{6 \div 3} = \frac{\$5}{2} = \frac{\$2.50}{1c}$

Total cost =  $y$   
 #cupcakes =  $x$

$k = \text{constant of prop.}$

$y = kx$

**Practice & Problem Solving**

7. What is the constant of proportionality in the equation  $y = 5x$ ?  $k = 5$

8. What is the constant of proportionality in the equation  $y = 0.41x$ ?  $k = 0.41$

**The constant of proportionality is 5.**

10. Model with Math in a chemical compound. There are 3 parts zinc for every 16 parts copper, by mass. A piece of the compound contains 320 grams of copper. Write and solve an equation to determine the amount of zinc in the chemical compound.

11. The weight of 3 eggs is shown. Assuming the three eggs are all the same weight, find the constant of proportionality.

12. The height of a stack of DVD cases is proportional to the number of cases in the stack. The height of 6 DVD cases is 114 mm.

a. Write an equation that relates the height,  $y$ , of a stack of DVD cases and the number of cases,  $x$ , in the stack.

b. What would be the height of 13 DVD cases?

13. Ann's car can travel 228 miles on 6 gallons of gas.

a. Write an equation to represent the distance,  $y$ , in miles Ann's car can travel on  $x$  gallons of gas.

b. Ann's car used 7 gallons of gas during a trip. How far did Ann drive?

*Handwritten notes:*

$y = 5x$

$k \cdot x$   
 $9 \cdot 7$

$y = 19x$

The height of 13 DVD cases would be 247 mm

$y = 38x$

$228 = k \cdot 6$

$\frac{228}{6} = \frac{k}{6}$

$38 = k$

$k = 38$

$y = kx$

$y = 38x$

$y = 38(7)$

$y = 266 \text{ mi}$

Ann drove 266 mi on her trip.

*Other notes:* see notes, refer to 3-3 #9, ht. # cases,  $9 = k \cdot 6$ ,  $114 = k(6)$ ,  $19 = k$ , case is 19 mm,  $y = 19x$ ,  $228 = k(6)$ ,  $19(13)$ ,  $\begin{matrix} 19 \\ \times 13 \\ \hline 57 \\ +190 \\ \hline 247 \end{matrix}$

10) zinc  $\rightarrow$  copper

3	16	
6	10	32
9	10	48
:	:	:
:	:	:
:	:	:
:	:	:
?	:	320

$32 \cdot 20 = ?$

$16c \cdot 20 = 320c$

how much zinc in comp. 320g copper

There are 60g of zinc in the compound.

14. The value of a baseball player's rookie card began to increase once the player retired in 1996. The value has increased by \$2.52 each year since then.
- How much was the baseball card worth in 1997?
  - Construct Arguments: Why is there not a proportional relationship between the years since the player retired and the card value? Explain.

$d = r \cdot t$   
 $y = k \cdot x$

Value: \$2.46  
 +2.52  
 rate (speed)

mi  
 $d = r \cdot t$   
 min

15. Higher Order Thinking A car travels 24 miles in  $3\frac{1}{2}$  minutes at a constant speed.
- Write an equation to represent the distance the car travels,  $d$ , in miles for  $n$  minutes.
  - Write an equation to represent the distance the car travels,  $d$ , in miles for  $n$  hours.

min  $\rightarrow$  hr  
 $\div 60$

Assessment Practice

16. For every ten sheets of stickers you buy, the total cost increases \$20.50. An equation that relates the number of sheets purchased,  $x$ , and the total cost,  $y$ , of the stickers is  $y = \frac{20.50}{10}x$ . Use the equation you wrote to complete the table.

Number of Sheets ( $x$ )	Total Cost ( $y$ )
3	\$10.25
5	\$26.65
13	\$38.95
19	

17. 600,000 gallons of water pass through a given point along a river every minute. Which equation represents the amount of water,  $y$ , that passes through the point in  $x$  minutes?
- $x = 10,000y$
  - $y = 600,000x$
  - $y = 10,000x$
  - $y = 600,000 + x$

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15 b)  $K = \frac{2}{3} \div \frac{60}{1}$

$\frac{2}{3} \times \frac{1}{60}$

$\frac{k}{(hr)} = \frac{1}{90}$

$d = \frac{1}{90}h$

$2\frac{1}{3} = k \cdot (3\frac{1}{2})$   
 $\frac{2\frac{1}{3}}{3\frac{1}{2}} = k$   
 $\frac{7}{3} \div \frac{7}{2}$   
 $\frac{7}{3} \times \frac{2}{7}$   
 $\frac{2}{3}$  miles per minute

