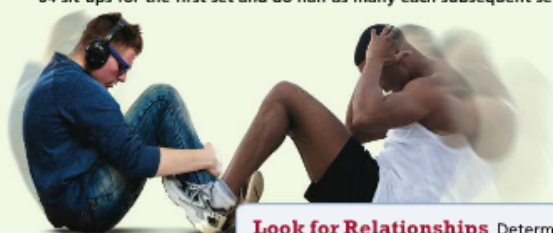


Explore It!



Calvin and Mike do sit-ups when they work out. They start with 64 sit-ups for the first set and do half as many each subsequent set.



Lesson 2-7
More Properties of Integer Exponents

Go Online | PearsonRealize.com

I can...
write a number with a negative or zero exponent a different way.

Look for Relationships Determine whether the relationship shown for Set 1 is also true for Sets 2–5.

A. What representation can you use to show the relationship between the set number and the number of sit-ups?

B. What conclusion can you make about the relationship between the number of sit-ups in each set?

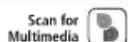
Focus on math practices

Use Structure How could you determine the number of sit-up sets Calvin and Mike do?

Essential Question What do the Zero Exponent and Negative Exponent Properties mean?



EXAMPLE 1 The Zero Exponent Property



Marchella is playing a card-matching game with some classmates. Four matches have been made. It is Marchella's turn, and she chooses 3^0 . What card would complete her match?



Organize the information in a table and look for a pattern.

Exponent Form	Simplified Form
3^4	81
3^3	27
3^2	9
3^1	3
3^0	?

$\div 3$
 $\div 3$
 $\div 3$
 $\div 3$

As the exponent decreases by one, the product is divided by 3.

$3 \div 3 = 1$, so $3^0 = 1$.

ANOTHER WAY Use the Quotient of Powers Property.

$$3^3 \div 3^3 = 3^3 - 3^3 = 3^0$$

When dividing two exponential expressions with the same base, subtract the exponents.

and

$$\frac{3^3}{3^3} = \frac{3 \times 3 \times 3}{3 \times 3 \times 3} = 1$$

so $3^0 = 1$

The **Zero Exponent Property** states that $a^0 = 1$ (assuming $a \neq 0$).

Try It!

Evaluate.

- a. $(-7)^0$ b. $(43)^0$ c. 1^0 d. $(0.5)^0$

Convince Me! Why is $2(7^0) = 2$?

EXAMPLE 2**The Negative Exponent Property**Simplify the expression $4^3 \div 4^5$.

$$4^3 \div 4^5 = \frac{4^3}{4^5}$$

Remember, $\frac{4}{4} = 1$.

$$= \frac{4 \times 4 \times 4}{4 \times 4 \times 4 \times 4 \times 4} = \frac{1}{16}$$

and

$$4^3 \div 4^5 = 4^{(3-5)} = 4^{-2}$$

Use the Quotient of Powers Property.

$$\text{So, } 4^{-2} = \frac{1}{16}.$$

The **Negative Exponent Property** states that $a^{-n} = \frac{1}{a^n}$ (assuming $a \neq 0$).**Try It!**

Write each expression using positive exponents.

a. 8^{-2}

b. 2^{-4}

c. 3^{-5}

EXAMPLE 3**Expressions with Negative Exponents**Write the expression $\frac{1}{7^{-3}}$ with a positive exponent.

$$\frac{1}{7^{-3}} = \frac{1}{\frac{1}{7^3}}$$

Use the Negative Exponent Property.

$$= 1 \cdot \frac{7^3}{1}$$

$$= 7^3$$

Multiply by the reciprocal of the denominator.

**Try It!**

Write each expression using positive exponents.

a. $\frac{1}{5^{-3}}$

b. $\frac{1}{2^{-6}}$



Name: _____

Squares and Square Roots

Date: _____

n	Squared ² n ²	Square Root \sqrt{n}
1	1	1.000
2	4	1.414
3	9	1.732
4	16	2.000
5	25	2.236
6	36	2.449
7	49	2.646
8	64	2.828
9	81	3.000
10	100	3.162
11	121	3.317
12	144	3.464
13	169	3.606
14	196	3.742
15	225	3.873
16	256	4.000
17	289	4.123
18	324	4.243
19	361	4.359
20	400	4.472
21	441	4.583
22	484	4.690
23	529	4.796
24	576	4.899
25	625	5.000
26	676	5.099
27	729	5.196
28	784	5.292
29	841	5.385
30	900	5.477
31	961	5.568
32	1024	5.657
33	1089	5.745
34	1156	5.831
35	1225	5.916
36	1296	6.000
37	1369	6.083
38	1444	6.164
39	1521	6.245
40	1600	6.325
41	1681	6.403
42	1764	6.481
43	1849	6.557
44	1936	6.633
45	2025	6.708
46	2116	6.782
47	2209	6.856
48	2304	6.928
49	2401	7.000
50	2500	7.071

n	Squared ² n ²	Square Root \sqrt{n}
51	2601	7.141
52	2704	7.211
53	2809	7.280
54	2916	7.348
55	3025	7.416
56	3136	7.483
57	3249	7.550
58	3364	7.616
59	3481	7.681
60	3600	7.746
61	3721	7.810
62	3844	7.874
63	3969	7.937
64	4096	8.000
65	4225	8.062
66	4356	8.124
67	4489	8.185
68	4624	8.246
69	4761	8.307
70	4900	8.367
71	5041	8.426
72	5184	8.485
73	5329	8.544
74	5476	8.602
75	5625	8.660
76	5776	8.718
77	5929	8.775
78	6084	8.832
79	6241	8.888
80	6400	8.944
81	6561	9.000
82	6724	9.055
83	6889	9.110
84	7056	9.165
85	7225	9.220
86	7396	9.274
87	7569	9.327
88	7744	9.381
89	7921	9.434
90	8100	9.487
91	8281	9.539
92	8464	9.592
93	8649	9.644
94	8836	9.695
95	9025	9.747
96	9216	9.798
97	9409	9.849
98	9604	9.899
99	9801	9.950
100	10000	10.000

n	Square Root \sqrt{n}
101	10.050
102	10.100
103	10.149
104	10.198
105	10.247
106	10.296
107	10.344
108	10.392
109	10.440
110	10.488
111	10.536
112	10.583
113	10.630
114	10.677
115	10.724
116	10.770
117	10.817
118	10.863
119	10.909
120	10.954
121	11.000
122	11.045
123	11.091
124	11.136
125	11.180
126	11.225
127	11.269
128	11.314
129	11.358
130	11.402
131	11.446
132	11.489
133	11.533
134	11.576
135	11.619
136	11.662
137	11.705
138	11.747
139	11.790
140	11.832
141	11.874
142	11.916
143	11.958
144	12.000
145	12.042
146	12.083
147	12.124
148	12.166
149	12.207
150	12.247

n	Square Root \sqrt{n}
151	12.288
152	12.329
153	12.369
154	12.410
155	12.450
156	12.490
157	12.530
158	12.570
159	12.610
160	12.649
161	12.689
162	12.728
163	12.767
164	12.806
165	12.845
166	12.884
167	12.923
168	12.961
169	13.000
170	13.038
171	13.077
172	13.115
173	13.153
174	13.191
175	13.229
176	13.266
177	13.304
178	13.342
179	13.379
180	13.416
181	13.454
182	13.491
183	13.528
184	13.565
185	13.601
186	13.638
187	13.675
188	13.711
189	13.748
190	13.784
191	13.820
192	13.856
193	13.892
194	13.928
195	13.964
196	14.000
197	14.036
198	14.071
199	14.107
200	14.142

n	Square Root \sqrt{n}
201	14.177
202	14.213
203	14.248
204	14.283
205	14.318
206	14.353
207	14.387
208	14.422
209	14.457
210	14.491
211	14.526
212	14.560
213	14.595
214	14.629
215	14.663
216	14.697
217	14.731
218	14.765
219	14.799
220	14.832
221	14.866
222	14.900
223	14.933
224	14.967
225	15.000
226	15.033
227	15.067
228	15.100
229	15.133
230	15.166
231	15.199
232	15.232
233	15.264
234	15.297
235	15.330
236	15.362
237	15.395
238	15.427
239	15.460
240	15.492
241	15.524
242	15.556
243	15.588
244	15.620
245	15.652
246	15.684
247	15.716
248	15.748
249	15.780
250	15.811

KEY CONCEPT

KEY
CONCEPT

Use these additional properties when simplifying or generating equivalent expressions with exponents (when $a \neq 0$ and $n \neq 0$).

Zero Exponent Property

$$a^0 = 1$$

Negative Exponent Property

$$a^{-n} = \frac{1}{a^n}$$

Do You Understand?

- Essential Question** What do the Zero Exponent and Negative Exponent Properties mean?
- Reasoning** In the expression 9^{-12} , what does the negative exponent mean?
- Reasoning** In the expression $3(2^0)$, what is the order of operations? Explain how you would evaluate the expression.

Do You Know How?

- Simplify $1,999,999^0$.
- Write 7^{-6} using a positive exponent.
 - Rewrite $\frac{1}{10^{-3}}$ using a positive exponent.
- Evaluate $27x^0y^{-2}$ for $x = 4$ and $y = 3$.



Name: _____







Practice & Problem Solving

Leveled Practice In 7–8, complete each table to find the value of a nonzero number raised to the power of 0.

7.

Exponent	Simplified
4^4	256
4^3	<input type="text"/>
4^2	<input type="text"/>
4^1	<input type="text"/>
4^0	<input type="text"/>

8.

Exponent	Simplified
$(-2)^4$	16
$(-2)^3$	<input type="text"/>
$(-2)^2$	<input type="text"/>
$(-2)^1$	<input type="text"/>
$(-2)^0$	<input type="text"/>

9. Given: $(-3.2)^0$

- Simplify the given expression.
- Write two expressions equivalent to the given expression. Explain why the three expressions are equivalent.

10. Simplify each expression for $x = 6$.

- $12x^0(x^{-4})$
- $14(x^{-2})$

In 11 and 12, compare the values using $>$, $<$, or $=$.

11. 3^{-2} 1

12. $(\frac{1}{4})^0$ 1

In 13 and 14, rewrite each expression using a positive exponent.

13. 9^{-4}

14. $\frac{1}{2^{-6}}$

15. Given: $9y^0$

- Simplify the expression for $y = 3$.
- Construct Arguments** Will the value of the given expression vary depending on y ? Explain.

16. Simplify each expression for $x = 4$.

a. $-5x^{-4}$

b. $7x^{-3}$

17. Evaluate each pair of expressions.

a. $(-3)^{-8}$ and -3^{-8}

b. $(-3)^{-9}$ and -3^{-9}

18. **Be Precise** To win a math game, Lamar has to pick a card with an expression that has a value greater than 1. The card Lamar chooses reads $(\frac{1}{2})^{-4}$. Does Lamar win the game? Explain.



19. Simplify the expression. Assume that x is nonzero. Your answer should have only positive exponents.
 $x^{-10} \cdot x^6$

20. **Higher Order Thinking**

a. Is the value of the expression $(\frac{1}{4})^{-2}$ greater than 1, equal to 1, or less than 1?

b. If the value of the expression is greater than 1, show how you can change one sign to make the value less than 1. If the value is less than 1, show how you can change one sign to make the value greater than 1. If the value is equal to 1, show how you can make one change to make the value not equal to 1.

Assessment Practice

21. Rewrite 5^{-3} using a positive exponent.

22. Which expressions have values less than 1 when $x = 4$? Select all that apply.

$(\frac{3}{x^2})^0$

x^0

$\frac{1}{6^{-x}}$

$\frac{1}{x^{-3}}$

$3x^{-4}$

