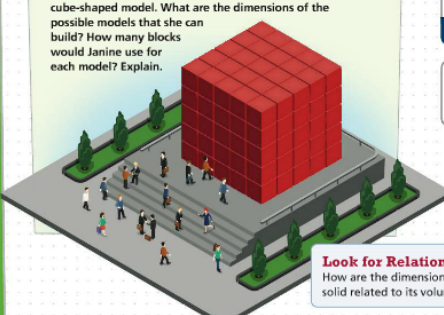


Solve & Discuss It!

Janine can use up to 150 one-inch blocks to build a solid, cube-shaped model. What are the dimensions of the possible models that she can build? How many blocks would Janine use for each model? Explain.



Look for Relationships
How are the dimensions of a solid related to its volume?

Lesson 2-5

Solve Equations Using Square Roots and Cube Roots

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I can...
solve equations involving squares or cubes.

Focus on math practices

Reasoning Janine wants to build a model using $\frac{1}{2}$ -inch cubes. How many $\frac{1}{2}$ -inch cubes would she use to build a solid, cube-shaped model with side lengths of 4 inches? Show your work.

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Essential Question

How can you solve equations with squares and cubes?



INTERACTIVE SERVICES

Scan for Multimedia


EXAMPLE 1

Solve Equations Involving Perfect Squares

Darius is restoring a square tabletop. He wants to finish the outside edges with a piece of decorative molding. What total length of molding will Darius need?

Draw a diagram to represent the tabletop.



Use the formula $A = s^2$ to find each side length. To solve, take the square root of both sides of the equation.

$$A = s^2$$

$$25 = s^2$$

$$\sqrt{25} = \sqrt{s^2}$$

$$\pm 5 = s$$


Because $5^2 = 5 \times 5 = 25$ and $(-5)^2 = -5 \times -5 = 25$, $s = 5$ and $s = -5$, or $s = \pm 5$.

Since length is positive, each side length of the tabletop is 5 feet. Darius needs 20 feet of decorative molding.

Generalize In general, an equation of the form $x^2 = p$, where p is a positive rational number, has two solutions, $x = \pm \sqrt{p}$.

Try It!

What is the side length, s , of the square below?



$A = s^2$
 = s^2
 = $\sqrt{s^2}$
 \pm = s

Each side of the square measures meters.

Convince Me! Why are there two possible solutions to the equation $s^2 = 100$? Explain why only one of the solutions is valid in this situation.

110 2-5 Solve Equations Using Square Roots and Cube Roots
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EXAMPLE 2 Solve Equations Involving Perfect Cubes

Kyle has a large, cube-shaped terrarium for his iguana. He wants to cover the opening with a square screen. What are the dimensions, s , for the screen?

$$V = s^3$$

$$343 = s^3$$

$$\sqrt[3]{343} = \sqrt[3]{s^3}$$

$$7 = s$$

The value of s is not $\pm \sqrt[3]{343}$ because $(-7)^3 = -7 \times -7 \times -7 = -343$.

Each edge of the terrarium is 7 feet, so the dimensions of the screen are 7 feet by 7 feet.



Try It!

Solve $x^3 = 64$.

EXAMPLE 3 Solve Equations Involving Imperfect Squares and Cubes

Solve for x .

A. $x^2 = 50$
 $\sqrt{x^2} = \sqrt{50}$
 $x = \pm \sqrt{50}$

Because 50 is not a perfect square, write the solution using the square root symbol.

There are two possible solutions, $x = +\sqrt{50}$ and $x = -\sqrt{50}$.

B. $x^3 = 37$
 $\sqrt[3]{x^3} = \sqrt[3]{37}$
 $x = \sqrt[3]{37}$

$x = \sqrt[3]{37}$ is an exact solution of the equation.

There is one possible solution, $x = \sqrt[3]{37}$.

Try It!

a. Solve $a^3 = 11$.

b. Solve $c^2 = 27$.

Name: _____ Squares and Square Roots Date: _____

n	Squared n ²	Square Root \sqrt{n}	n	Squared n ²	Square Root \sqrt{n}	n	Square Root \sqrt{n}	n	Square Root \sqrt{n}	n	Square Root \sqrt{n}
1	1	1.000	51	2601	7.141	101	10.050	151	12.288	201	14.177
2	4	1.414	52	2704	7.211	102	10.100	152	12.329	202	14.213
3	9	1.732	53	2809	7.280	103	10.149	153	12.369	203	14.248
4	16	2.000	54	2916	7.348	104	10.198	154	12.410	204	14.283
5	25	2.236	55	3025	7.416	105	10.247	155	12.450	205	14.318
6	36	2.449	56	3136	7.483	106	10.296	156	12.490	206	14.353
7	49	2.646	57	3249	7.550	107	10.344	157	12.530	207	14.387
8	64	2.828	58	3364	7.616	108	10.392	158	12.570	208	14.422
9	81	3.000	59	3481	7.681	109	10.440	159	12.610	209	14.457
10	100	3.162	60	3600	7.746	110	10.488	160	12.649	210	14.491
11	121	3.317	61	3721	7.810	111	10.536	161	12.689	211	14.525
12	144	3.464	62	3844	7.874	112	10.583	162	12.728	212	14.560
13	169	3.606	63	3969	7.937	113	10.630	163	12.767	213	14.595
14	196	3.742	64	4096	8.000	114	10.677	164	12.806	214	14.629
15	225	3.873	65	4225	8.062	115	10.724	165	12.845	215	14.663
16	256	4.000	66	4356	8.124	116	10.770	166	12.884	216	14.697
17	289	4.123	67	4489	8.185	117	10.817	167	12.923	217	14.731
18	324	4.243	68	4624	8.246	118	10.863	168	12.961	218	14.765
19	361	4.359	69	4761	8.307	119	10.909	169	13.000	219	14.799
20	400	4.472	70	4900	8.367	120	10.954	170	13.038	220	14.832
21	441	4.583	71	5041	8.426	121	11.000	171	13.077	221	14.865
22	484	4.690	72	5184	8.485	122	11.045	172	13.115	222	14.900
23	529	4.796	73	5329	8.544	123	11.091	173	13.153	223	14.933
24	576	4.899	74	5476	8.602	124	11.136	174	13.191	224	14.967
25	625	5.000	75	5625	8.660	125	11.180	175	13.229	225	15.000
26	676	5.099	76	5776	8.718	126	11.225	176	13.266	226	15.033
27	729	5.196	77	5929	8.775	127	11.269	177	13.304	227	15.067
28	784	5.292	78	6084	8.832	128	11.314	178	13.342	228	15.100
29	841	5.385	79	6241	8.888	129	11.358	179	13.379	229	15.133
30	900	5.477	80	6400	8.944	130	11.402	180	13.416	230	15.166
31	961	5.568	81	6561	9.000	131	11.446	181	13.454	231	15.199
32	1024	5.657	82	6724	9.055	132	11.489	182	13.491	232	15.232
33	1089	5.745	83	6889	9.110	133	11.533	183	13.528	233	15.264
34	1156	5.831	84	7056	9.165	134	11.576	184	13.565	234	15.297
35	1225	5.916	85	7225	9.220	135	11.619	185	13.601	235	15.330
36	1296	6.000	86	7396	9.274	136	11.662	186	13.638	236	15.362
37	1369	6.083	87	7569	9.327	137	11.705	187	13.675	237	15.395
38	1444	6.164	88	7744	9.381	138	11.747	188	13.711	238	15.427
39	1521	6.245	89	7921	9.434	139	11.790	189	13.748	239	15.460
40	1600	6.325	90	8100	9.487	140	11.832	190	13.784	240	15.492
41	1681	6.403	91	8281	9.539	141	11.874	191	13.820	241	15.524
42	1764	6.481	92	8464	9.592	142	11.916	192	13.856	242	15.556
43	1849	6.557	93	8649	9.644	143	11.958	193	13.892	243	15.588
44	1936	6.633	94	8836	9.695	144	12.000	194	13.928	244	15.620
45	2025	6.708	95	9025	9.747	145	12.042	195	13.964	245	15.652
46	2116	6.782	96	9216	9.798	146	12.083	196	14.000	246	15.684
47	2209	6.856	97	9409	9.849	147	12.124	197	14.036	247	15.716
48	2304	6.928	98	9604	9.899	148	12.166	198	14.071	248	15.748
49	2401	7.000	99	9801	9.950	149	12.207	199	14.107	249	15.780
50	2500	7.071	100	10000	10.000	150	12.247	200	14.142	250	15.811

KEY CONCEPT

You can use square roots to solve equations involving squares.

$$\sqrt{81} = \pm 9 \cdot 9$$

$$\downarrow \quad \downarrow$$

$$x = \pm \sqrt{a}, \pm \sqrt{-a}$$

You can use cube roots to solve equations involving cubes.

$$\sqrt[3]{x^3} = \sqrt[3]{b}$$

$$\downarrow \quad \downarrow$$

$$x = \sqrt[3]{b}$$

Do You Understand?

1. **Essential Question** How can you solve equations with squares and cubes?

2. **Be Precise** Suri solved the equation $x^2 = 49$ and found that $x = 7$. What error did Suri make?

$$7 \cdot 7 = 49$$

$$-7(-7) = 49$$

Suri failed to account for the negative root.

3. **Construct Arguments** There is an error in the work shown below. Explain the error and provide a correct solution.

$$x^3 = 125$$

$$\sqrt[3]{x^3} = \sqrt[3]{125}$$

$$x = 5 \text{ and } x = -5$$

4. Why are the solutions to $x^2 = 17$ irrational?

Do You Know How?

5. If a cube has a volume of 27 cubic centimeters, what is the length of each edge? Use the volume formula $V = s^3$ and show your work.

$$V = 27 \text{ cm}^3$$

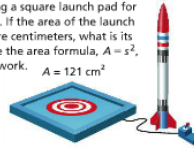
$$s^3 = 27 \text{ cm}^3$$

$$\sqrt[3]{s^3} = \sqrt[3]{27 \text{ cm}^3}$$

$$s = 3 \cdot 3 \cdot 3$$

Each edge is 3 cm.

6. Darius is building a square launch pad for a rocket project. If the area of the launch pad is 121 square centimeters, what is its side length? Use the area formula, $A = s^2$, and show your work.



$$A = 121 \text{ cm}^2$$

$$s^2 = 121$$

$$\sqrt{s^2} = \sqrt{121}$$

$$s = 11$$

7. Solve the equation $x^3 = -215$.

Practice & Problem Solving

Leveled Practice In 8 and 9, solve.

8. $z^2 = 1$

$$\sqrt{\square} = \sqrt{\square}$$

$$z = \pm \square$$

The solutions are \square and \square .

9. $a^3 = 216$

$$\sqrt[3]{a^3} = \sqrt[3]{216}$$

$$a = 6$$

10. Solve $v^2 = 47$.

$$\sqrt{v^2} = \sqrt{47}$$

$$v = \pm 6.9$$

12. Solve the equation $y^2 = 81$.

11. The area of a square photo is 9 square inches. How long is each side of the photo?

13. Solve the equation $w^3 = 1,000$.

14. The area of a square garden is shown. How long is each side of the garden?



15. Solve $b^2 = 77$.

16. Find the value of c in the equation $c^3 = 1,728$.

17. Solve the equation $v^3 = 12$.

Handwritten notes for problem 9:

$$216$$

$$\begin{array}{r} 4 \\ \times 54 \\ \hline 216 \end{array}$$

Handwritten notes for problem 11:

$$\sqrt{9} = 3$$

$$\frac{\sqrt[3]{8}}{\sqrt[3]{27}} = \frac{\sqrt[3]{2 \cdot 2 \cdot 2}}{\sqrt[3]{3 \cdot 3 \cdot 3}}$$

18. Higher Order Thinking Explain why $\sqrt[3]{-\frac{8}{27}}$ is $-\frac{2}{3}$.

$$\left(-\frac{2}{3}\right)\left(-\frac{2}{3}\right)\left(-\frac{2}{3}\right) = -\frac{8}{27}$$

19. Critique Reasoning Manolo says that the solution of the equation $g^2 = 36$ is $g = 6$ because $6 \times 6 = 36$. Is Manolo's reasoning complete? Explain.

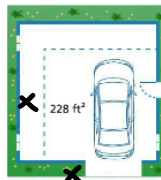
20. Evaluate $\sqrt[3]{-512}$.

- Write your answer as an integer.
- Explain how you can check that your result is correct.

21. Yael has a square-shaped garage with 228 square feet of floor space. She plans to build an addition that will increase the floor space by 50%. What will be the length, to the nearest tenth, of one side of the new garage?

+50%
0.5

$$100\% + 50\% = 1.5(228) = 342 \text{ ft}^2 \text{ (after exp)}$$



$$x^2 = \sqrt{342}$$

$$x \approx 18.49$$

$$x \approx 18.5 \text{ ft}$$

Assessment Practice

- The Travers are adding a new room to their house. The room will be a cube with a volume of 6,859 cubic feet. They are going to put in hardwood floors, which costs \$10 per square foot. How much will the hardwood floors cost?
- While packing for their cross-country move, the Chen family uses a crate that has the shape of a cube.

PART A

If the crate has the volume $V = 64$ cubic feet, what is the length of one edge?

PART B

The Chens want to pack a large, framed painting. If the framed painting has the shape of a square with an area of 12 square feet, will the painting fit flat against a side of the crate? Explain.

